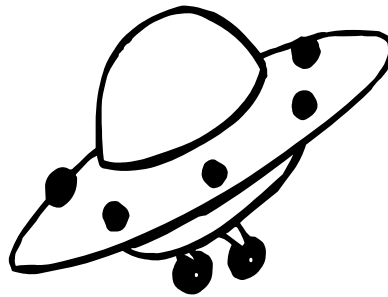
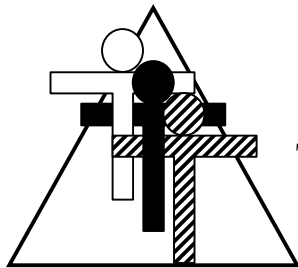


# Solving Systems of Equations



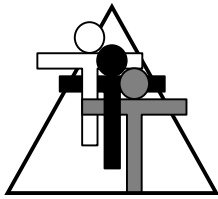
By Brad Fulton  
2005 CLMS Educator of the Year



Teacher to Teacher Press  
P.O. Box 233  
Millville, CA 96062  
[www.tttpress.com](http://www.tttpress.com)

Ph. (530) 547-4687  
[brad@tttpress.com](mailto:brad@tttpress.com)

Fax: (530) 547-4317  
[bill@tttpress.com](mailto:bill@tttpress.com)



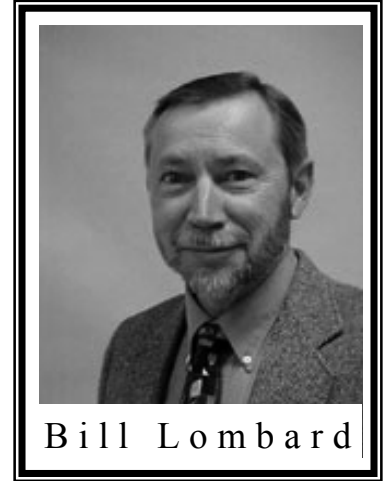
## Brad Fulton and Bill Lombard *Teacher to Teacher Press*

*"Building Mathematical Skill on a Foundation of Understanding"*



Brad Fulton

- ◆ **Consultants**
- ◆ **Educators**
- ◆ **Authors**
- ◆ **Seminar leaders**
- ◆ **Teacher trainers**
- ◆ **Conference speakers**



Bill Lombard

PO Box 233, Millville, CA 96062  
(530) 547-4687 [brad@tttpress.com](mailto:brad@tttpress.com)

5885 Avery Way, Redding, CA 96003  
(530) 243-2064 [bill@tttpress.com](mailto:bill@tttpress.com)

Known throughout the country for motivating and engaging teachers and students, Brad and Bill have authored over ten books that provide easy-to-teach yet mathematically-rich activities for busy teachers. In addition, they have co-authored six teacher training manuals full of activities and ideas that help teachers who believe mathematics must be both meaningful and powerful.

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*References available upon request*

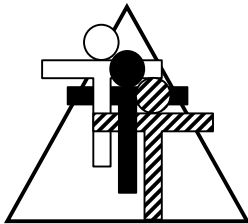
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This resource manual is dedicated to the students of Brad Fulton and Bill Lombard, who have been sources of inspiration to us as teachers. Without these students our lives would not be as rich and rewarding as they are.

For consultant services contact us at

Brad Fulton  
PO Box 233  
Millville, CA 96062  
Phone: (530) 547-4687  
Fax: (530) 547-4317  
brad@tttpress.com

Bill Lombard  
5885 Avery Way  
Redding, CA 96003  
Phone: (530) 243-2064  
Fax: (530) 242-1852  
bill@tttpress.com



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- ☑ Allows students to work with two variables painlessly
- ☑ Helps students solve for two unknowns
- ☑ Adaptable for grades 2 through 10!
- ☑ Demonstrates dependent and independent variables
- ☑ Incorporates multiple representations
- ☑ Leads students into the  $Ax+By=C$  form
- ☑ Makes a seamless transition to simultaneous equations
- ☑ Shows the interconnections between graphs, t-tables, and data charts
- ☑ Easy and fun!





## Money from Mars

### An Algebraic Solution (problem 1)

$$3g + 2b = 24$$

$$1g + 2b = 16$$

$$\begin{array}{r} 3g + 2b = 24 \\ - (1g + 2b = 16) \quad \text{Subtract} \\ \hline \end{array}$$

$$\frac{2g}{2} = \frac{8}{2}$$

Divide by the coefficient.

$$g = 4$$

$$3(4) + 2b = 24 \quad \text{Substitute.}$$

$$12 + 2b = 24 \quad \text{Multiply}$$

$$12 + 2b = 24$$

$$\begin{array}{r} -12 \quad -12 \\ \hline \end{array} \quad \text{Subtract.}$$

$$\frac{2b}{2} = \frac{12}{2}$$

Divide by the coefficient

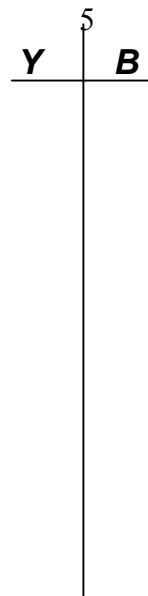
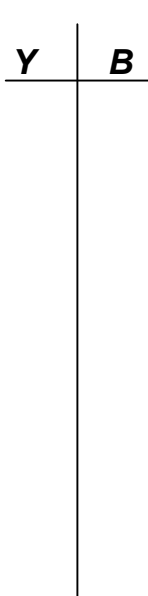
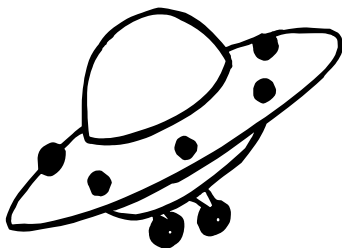
$$b = 6$$



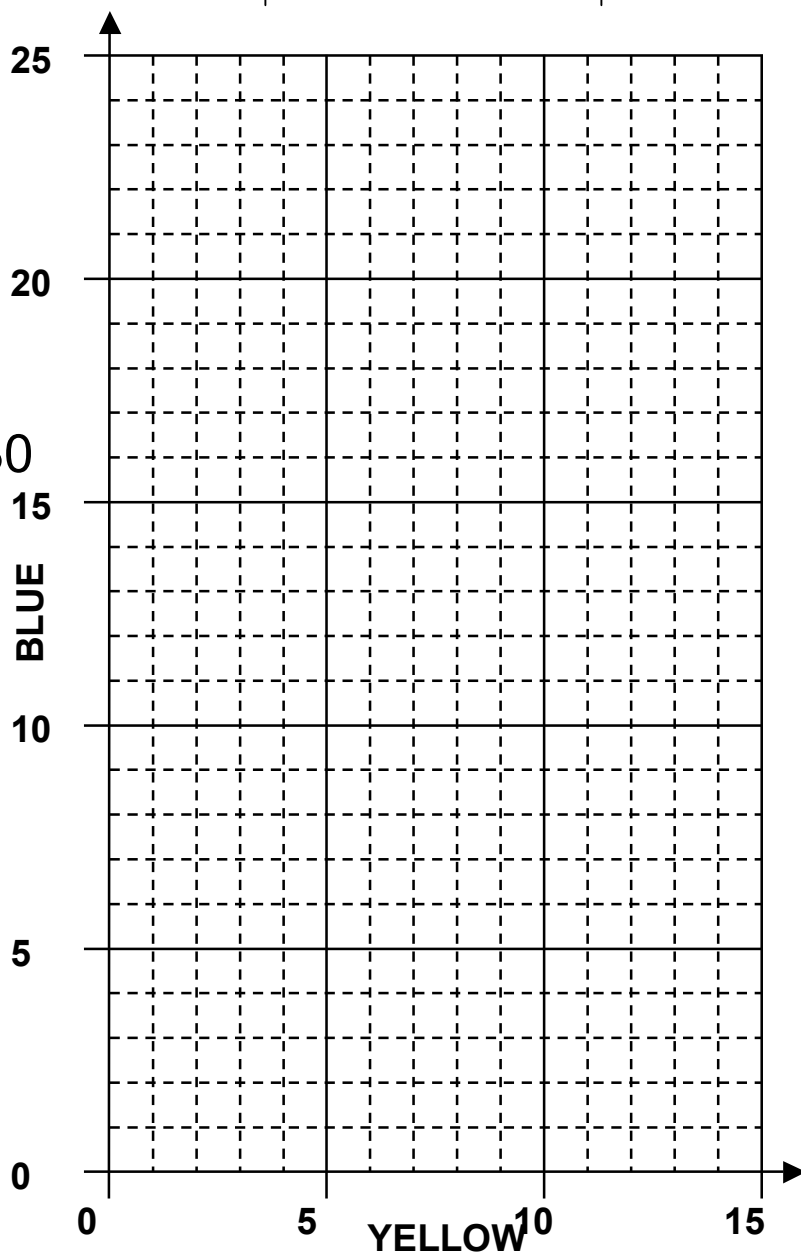
Name \_\_\_\_\_

### Money from Mars 3

$(Y)(Y)(B) = 14$

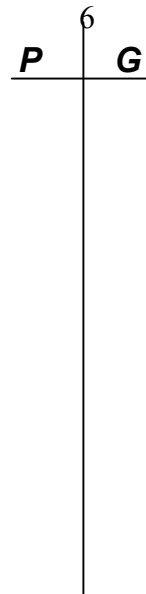
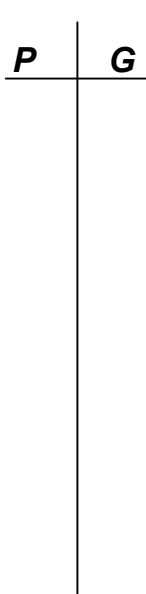
$(Y)(Y)(B)(B)(B)(B)(B) = 30$

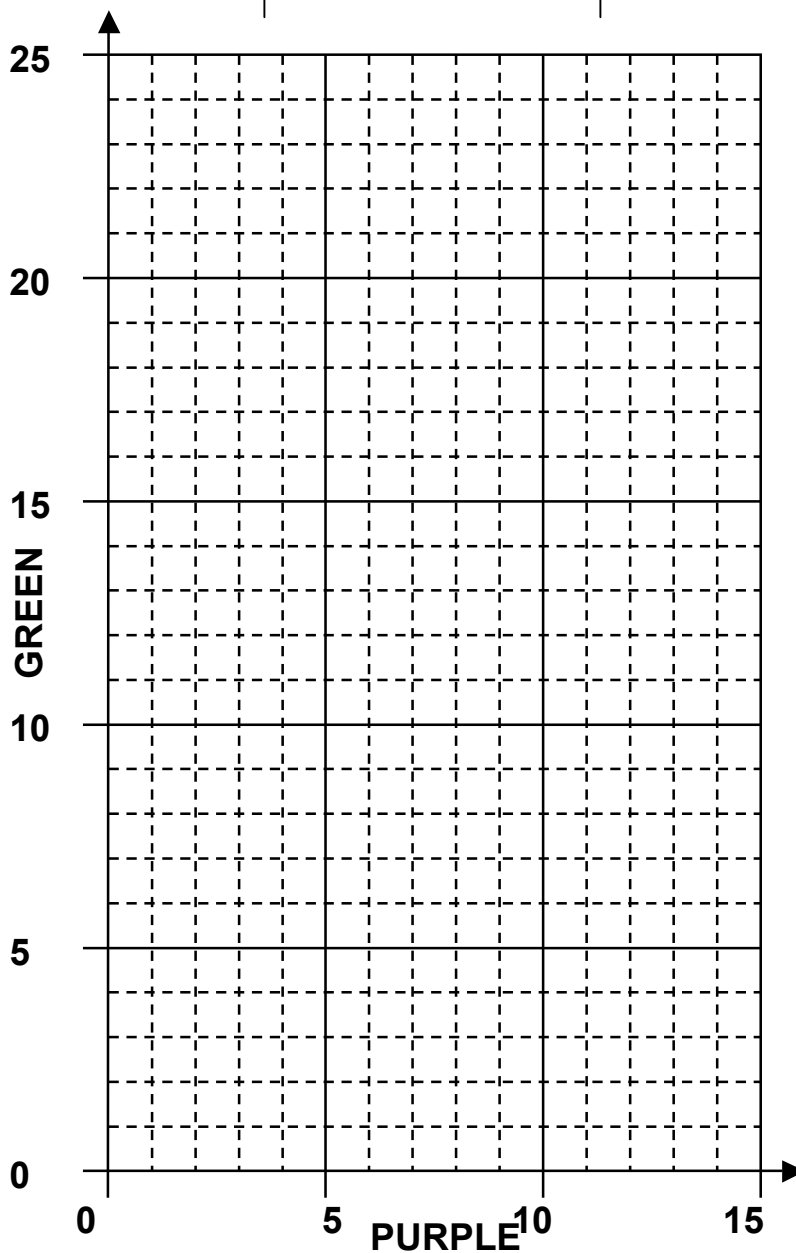
Name \_\_\_\_\_

### Money from Mars 4

$(P)(P)(P)(G) = 15$

$(P)(P)(G)(G)(G) = 24$

Name \_\_\_\_\_

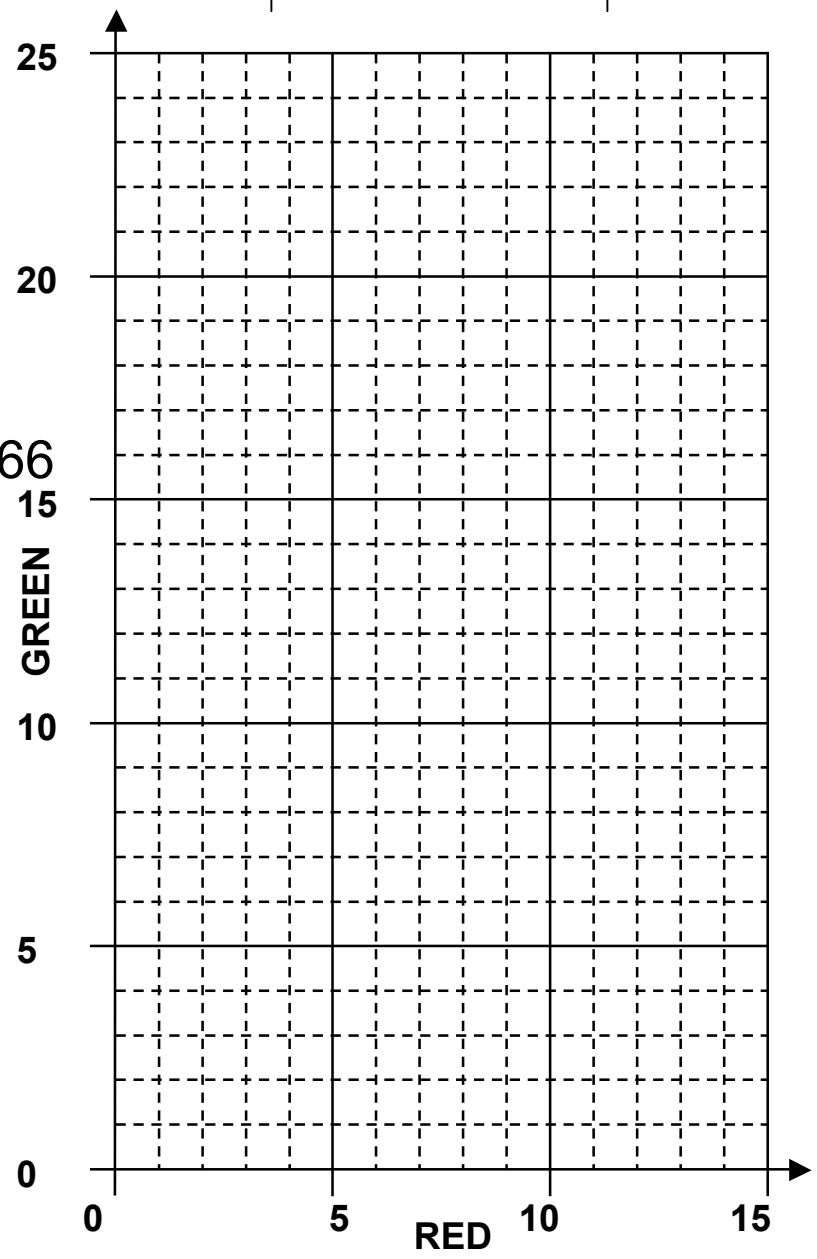
# Money from Mars 5



<i>R</i>	<i>G</i>	<i>R</i>	<i>G</i> <sup>7</sup>

(R) (R) (R) (R) (G) (G) (G) = 48


(R) (R) (G) (G) (G) (G) (G) = 66

## Money from Mars

### An Algebraic Solution (problem 5)

$$4r + 3g = 48$$

$$2r + 5g = 66 \quad \text{Multiply the second equation by 2.}$$

$$4r + 10g = 132$$

$$\underline{4r + 3g = 48} \quad \text{Subtract the first equation.}$$

$$\frac{7g}{7} = \frac{84}{7}$$

Divide by the coefficient.

$$g = 12$$

$$4r + 3(12) = 48 \quad \text{Substitute.}$$

$$4r + 36 = 48 \quad \text{Multiply}$$

$$4r + 36 = 48$$

$$\underline{-36 \quad -36} \quad \text{Subtract.}$$

$$\underline{4r} = \underline{12}$$

$$\frac{4r}{4} = \frac{12}{4}$$

Divide by the coefficient

$$r = 3$$

## Solutions

Problem 1:

$$3g + 2b = 24$$

$$g + 2b = 16$$

$$g = 4, b = 6$$

Problem 2

$$4p + 3r = 48$$

$$2p + 3r = 30$$

$$p = 9, r = 4$$

Problem 3

$$2y + 1b = 14$$

$$2y + 5b = 30$$

$$y = 5, b = 4$$

Problem 4

$$3p + 1g = 15$$

$$2p + 3g = 24$$

$$p = 3, g = 6$$

Problem 5

$$4r + 3g = 48$$

$$2r + 5g = 66$$

$$r = 3, g = 12$$

## Standards That May Be Taught Using Money from Mars

Grade	Standard	Description
2	Num. 5.1	Solve problems using combinations of coins and bills.
3	Alg. 2.1	Solve simple problems involving a functional relationship between two variables
4	Alg. 1.1	Use letters to stand for any number in simple expressions or equations.
5	Alg. 1.1	Use information taken from a graph or equation to answer questions about a problem situation
5	Alg. 1.1	Use a letter to represent an unknown number
5	Alg. 1.4	Identify and graph ordered pairs
5	Alg. 1.5	Solve problems involving linear functions
6	Alg. 1.3	Apply algebraic order of operations
6	Alg. 2.0	Students analyze tables, graphs, and rules to solve problems involving rates and proportions
7	Alg. 1.1	Use variables and appropriate operations to write an equation
7	Alg. 1.4	Use algebraic terminology
7	Alg. 1.5	Represent quantitative relationships graphically and interpret the meaning of a specific part of a graph
7	Alg. 3.3	Graph linear functions, noting that the vertical change per unit of horizontal change is called the slope
8	6.0	Graph a linear equation and compute the x- and y-intercepts
8	9.0	Students solve a system of linear equations in two variables algebraically and are able to interpret the answer graphically

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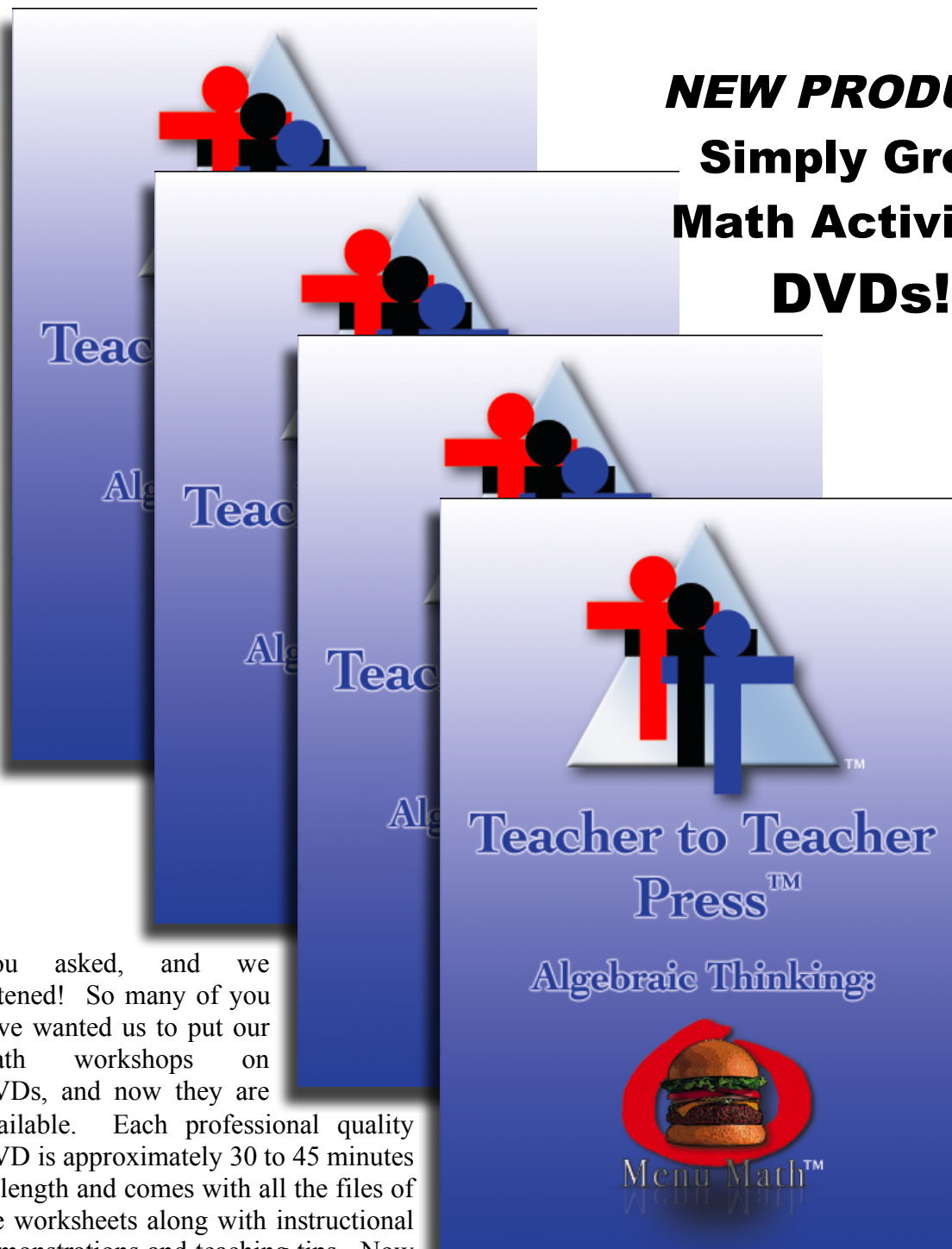
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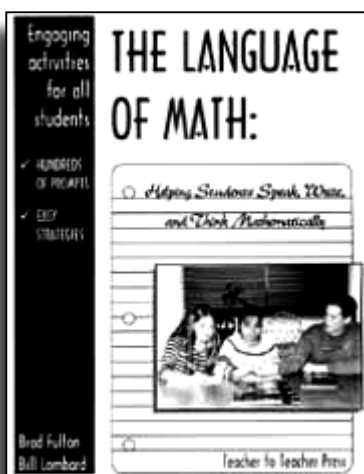


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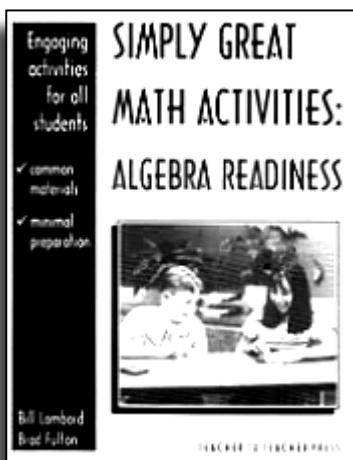
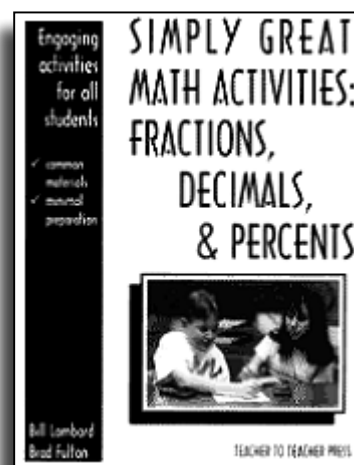
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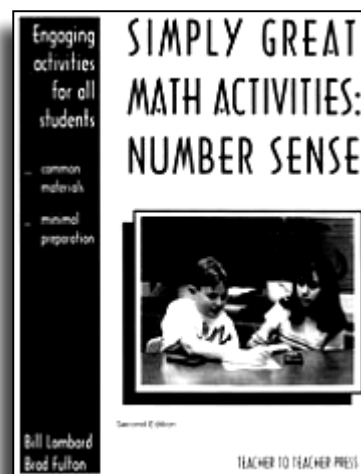
*The Language of Math helps teachers create a classroom environment rich in mathematical thinking by showing them how to easily incorporate oral and written language into their math classes. Over 100 journal and discussion starters are included along with extensive*

*Here are a dozen unique and conceptual activities that will help your students add, subtract, multiply and divide fractions as well as connect them to decimal and percent representations. Both you*



*Teachers are raving about how effective these activities have been in their classrooms. Children as young as fourth grade and college students alike say that algebra is easy and makes sense*

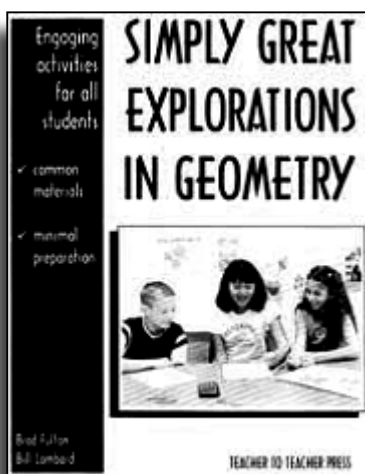
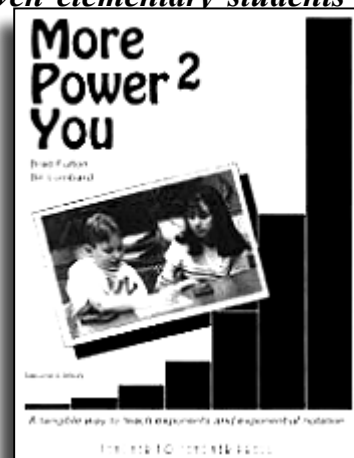
*Students don't even think they are doing math sometimes because these activities are so fun and engaging, but they are developing rich and valuable number sense as they explore these*





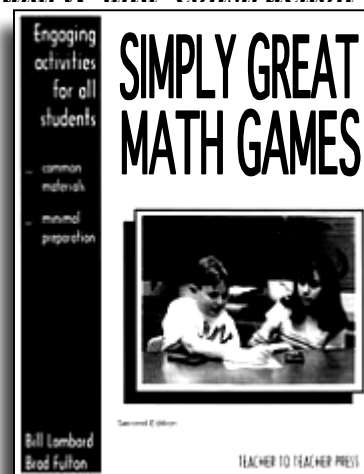
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*Exponents will finally make sense to your students after they participate in the unique activities found in this book. Both positive and negative exponents are demonstrated conceptually. Your students will even be able to explain why  $n^0 = 1$ .*



*Over one dozen geometry activities will excite your students as they discover the connections between geometry and fractions, decimals, percents, and even algebra. Area formulas, angle measurement, polygon attributes, vocabulary, and construction*

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